

EXPONENTIAL AND LOGARITHMIC FUNCTIONS

$$e^x = 0$$

$$e^x = \infty$$

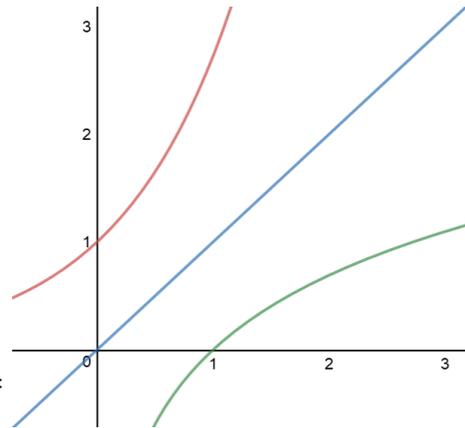
$$\ln \ln x = -\infty$$

$$\ln \ln x = \infty$$

$$\ln \ln x = x, \text{ where } \ln \ln e = 1$$

$$x = y \Leftrightarrow a^y = x$$

$$\ln \ln x = y \Leftrightarrow e^y =$$



Cancellation Equations

Laws of Logarithms

$$(a^x)^y = a^{xy}$$

$$a^x = x$$

$$(xy) = x + y$$

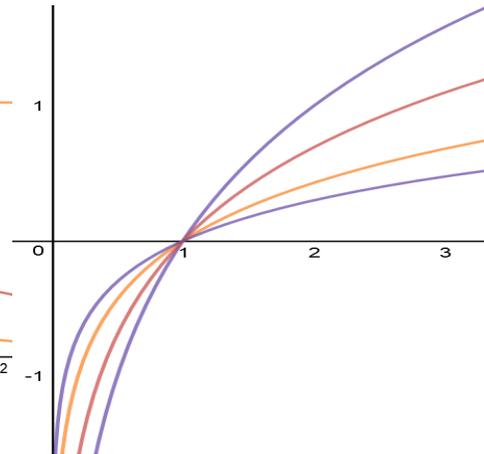
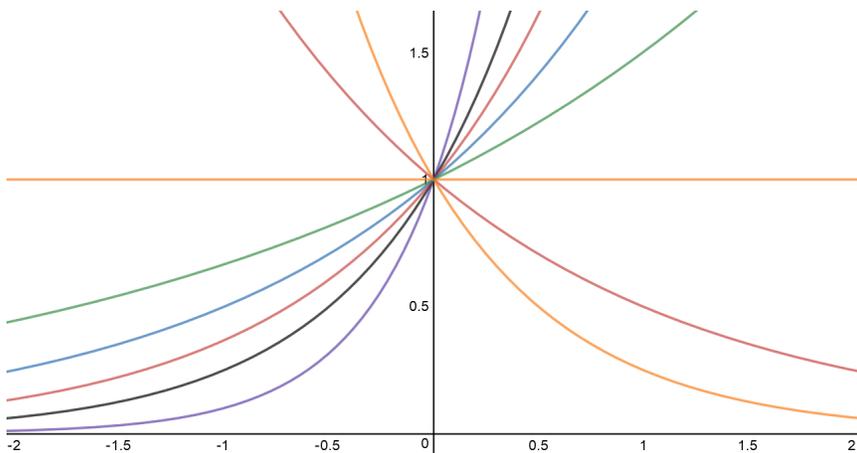
$$\ln \ln (e^x) = x$$

$$e^{\ln x} = x$$

$$\left(\frac{x}{y}\right) = x - y$$

$$= x$$

$$(x^r) = rx$$



HYPERBOLIC FUNCTIONS

$$\sinh x = \frac{e^x - e^{-x}}{2}$$

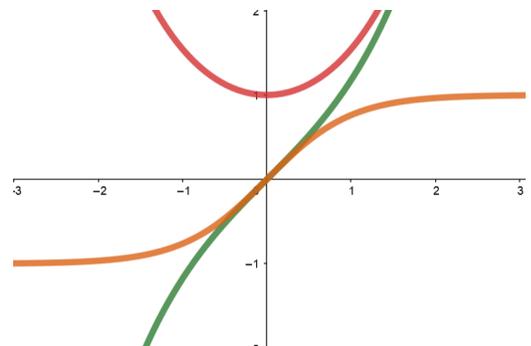
$$\cosh x = \frac{e^x + e^{-x}}{2}$$

$$\tanh x = \frac{\sinh x}{\cosh x}$$

$$\coth x = \frac{\cosh x}{\sinh x}$$

$$\frac{\sinh x}{\cosh x} = \tanh x$$

$$\frac{\cosh x}{\sinh x} = \coth x$$



INVERSE HYPERBOLIC FUNCTIONS

$$y = x \Leftrightarrow \sinh \sinh y = x$$

$$y = x \Leftrightarrow \cosh \cosh y = x \text{ and } y \geq 0$$

$$y = x \Leftrightarrow \tanh \tanh y = x$$

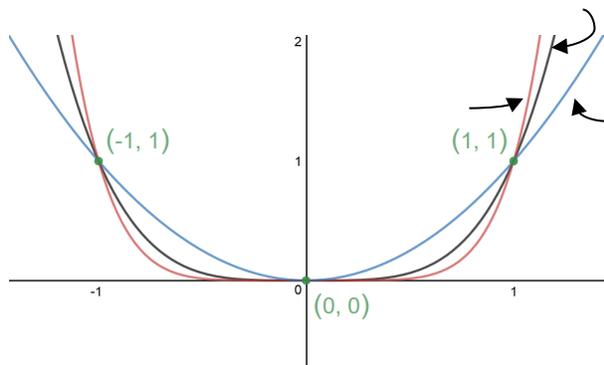
$$x = \ln \ln \left(x + \sqrt{x^2 + 1} \right)$$

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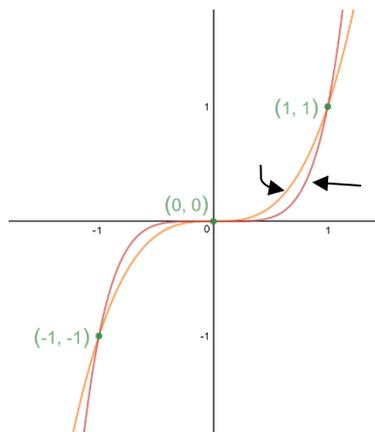
$$x = \ln \ln \left(\frac{1+x}{1-x} \right)$$

POWER FUNCTIONS $f(x) = x^n$

i. $f(x) = x^n$, where n is a positive integer

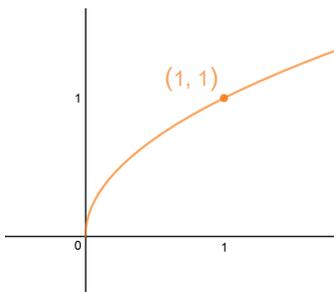


n is even

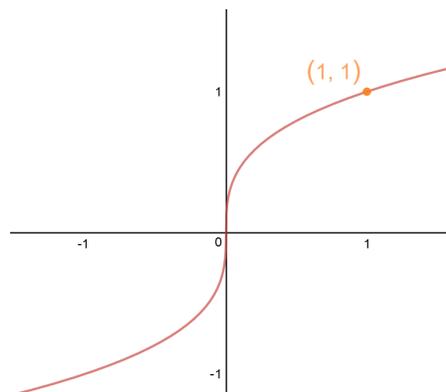


n is odd

ii. $f(x) = x^{\frac{1}{n}} = \sqrt[n]{x}$, where n is a positive integer

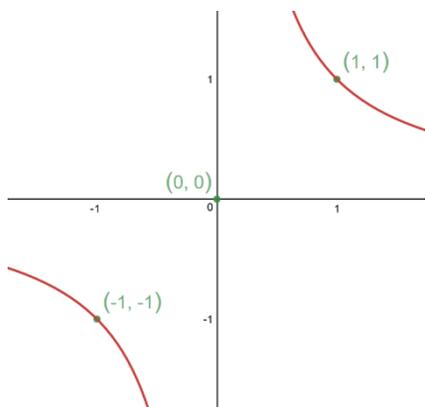


n is even



n is odd

iii. $f(x) = x^{-1} = \frac{1}{x}$



INVERSE TRIGONOMETRIC FUNCTIONS

$x = \sin y \Leftrightarrow \sin^{-1} x = y$ and

$x = \cos y \Leftrightarrow \cos^{-1} x = y$ and

$x = \tan y \Leftrightarrow \tan^{-1} x = y$ and

